## PHYS 160 - Homework \#5

## Model Signal

You are to help your scientific friend with her model of an electronic signal. She describes this signal via a Fourier Series as

$$
\begin{equation*}
\operatorname{signal}(N 1, N 2, t)=\sum_{n=N 1}^{N 2} \operatorname{term}(2 n-1, t) \tag{1}
\end{equation*}
$$

where $n$ is the sum index which ranges over the values from $N 1$ to $N 2$. The variable $t$ is the time. The $\operatorname{term}(n, t)$ function is defined as

$$
\begin{equation*}
\operatorname{term}(n, t)=a(n) \sin (2 \pi n t / T P) \tag{2}
\end{equation*}
$$

where $T P$ is the period of the signal and the amplitude $a(n)$ is

$$
\begin{equation*}
a(n)=\frac{4}{\pi} \frac{1}{n} \tag{3}
\end{equation*}
$$

## Using Maple

- Define signal $(N 1, N 2, t), \operatorname{term}(n, t)$ and $a(n)(i n$ this order, i.e., eq. 1, 2, and 3 ).
- Assign the constant: $T P=1.125$.
- As a check, plot the signal function, $\operatorname{signal}(N 1, N 2, t)$, with the first 50 terms included in the series starting from the fundamental frequency, $N 1=1$, over the time domain $t=[0,2 T P]$. Label this plot with a title.


## Minima and Maxima in Truncated Signals

A signal can be electronically modified, either on purpose or by accident (poor design or malfunction). In the language of the Fourier Series this corresponds to applying a filter to the signal to cut or modify either the low or high frequency terms, or both. A filter applies a modification to the signal by multiplying the amplitude $a(n)$ of each term in the Fourier Series by a filtering function that depends on $n$.

For example, consider the following high frequency filtering function

$$
\operatorname{filter}(n)=\frac{1}{1+\exp (n-9)}
$$

It is applied to the Fourier Series via

$$
\text { filtered_signal }(N 1, N 2, t)=\sum_{n=N 1}^{N 2} \text { filter }(2 n-1) \operatorname{term}(2 n-1, t)
$$

- Define filter ( $n$ )
- Define the filtered signal filtered_signal $(N 1, N 2, t)$.
- Plot this filtered signal for $N 1=1$ and $N 2=15$ over the time domain $t=[0, T P]$. Label this plot with a title.
- Calculate the slope function of this filtered signal.
- Plot the slope function over the time domain $t=[0, T P]$.
- Find the maxima and minima of the filtered signal over the first half of the cycle of the signal ( first half of the period ). Compute the times at which these occur as well as the values of the signal.
- Can you find any symmetry in the times and signal values you just found?
- How would you get the minima and maxima of the filtered signal in the second half of the signal without having to fsolve() for them?

