## Model Signal

You are to help your scientific friend with her model of an electronic signal. She describes this signal via a *Fourier Series* as

$$signal(N1, N2, t) = \sum_{n=N1}^{N2} term(2n-1, t)$$
 (1)

where n is the sum index which ranges over the values from N1 to N2. The variable t is the time. The term(n,t) function is defined as

$$term(n,t) = a(n)sin(2\pi nt/TP)$$
<sup>(2)</sup>

where TP is the *period of the signal* and the amplitude a(n) is

$$a(n) = \frac{4}{\pi} \frac{1}{n} \tag{3}$$

## Using Maple

- Define signal(N1, N2, t), term(n, t) and a(n) (in this order, i.e., eq. 1, 2, and 3).
- Assign the constant: TP = 1.125.
- As a check, plot the signal function, signal(N1, N2, t), with the first 50 terms included in the series starting from the fundamental frequency, N1 = 1, over the time domain t = [0, 2TP]. Label this plot with a title.

## Minima and Maxima in Truncated Signals

A signal can be electronically modified, either on purpose or by accident (poor design or malfunction). In the language of the Fourier Series this corresponds to applying a filter to the signal to cut or modify either the *low* or *high* frequency terms, or both. A filter applies a modification to the signal by multiplying the amplitude a(n) of each term in the Fourier Series by a filtering function that depends on n.

For example, consider the following high frequency filtering function

$$filter(n) = \frac{1}{1 + \exp(n - 9)}$$

It is applied to the Fourier Series via

$$filtered\_signal(N1, N2, t) = \sum_{n=N1}^{N2} filter(2n-1)term(2n-1, t)$$

- Define filter(n)
- Define the filtered signal  $filtered\_signal(N1, N2, t)$ .

- Plot this filtered signal for N1 = 1 and N2 = 15 over the time domain t = [0, TP]. Label this plot with a title.
- Calculate the *slope* function of this filtered signal.
- Plot the *slope* function over the time domain t = [0, TP].
- Find the maxima and minima of the filtered signal over the first half of the cycle of the signal ( first half of the period ). Compute the times at which these occur as well as the values of the signal.
- Can you find any symmetry in the times and signal values you just found?
- How would you get the minima and maxima of the filtered signal in the *second half* of the signal without having to *fsolve()* for them?