

The Topology of Chaos

Chapter 1: Overview

Robert Gilmore

Physics Department
Drexel University
Philadelphia, PA 19104
robert.gilmore@drexel.edu

Physics and Topology Workshop
Drexel University, Philadelphia, PA 19104

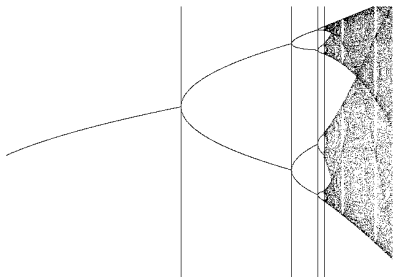
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J. R. Tredicce

Can you explain my data?

I dare you to explain my data!

Where is Tredicce coming from?



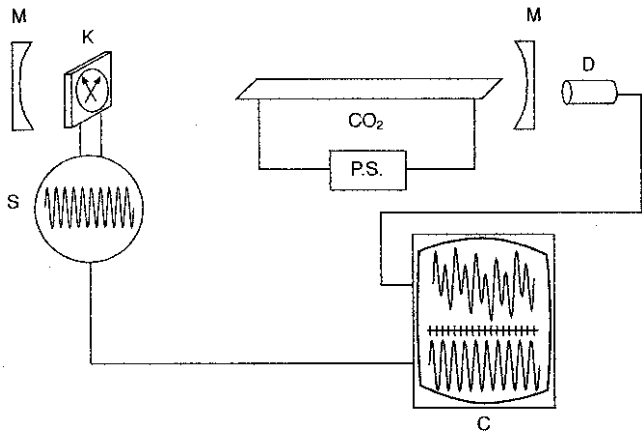
Feigenbaum:

$$\alpha = 4.66920\ 16091\ \dots$$

$$\delta = -2.50290\ 78750\ \dots$$

Experiment

LSA Experimental Arrangement



Original Objectives

Construct a simple, algorithmic procedure for:

- Classifying strange attractors
- Extracting classification information

from experimental signals.

Result

There is now a classification theory.

- 1 It is topological
- 2 It has a hierarchy of 4 levels
- 3 Each is discrete
- 4 There is rigidity and degrees of freedom
- 5 It is applicable to R^3 only — for now

The 4 Levels of Structure

- **Basis Sets of Orbits**
- **Branched Manifolds**
- **Bounding Tori**
- **Extrinsic Embeddings**

Organization

LINKS OF PERIODIC ORBITS

organize

BOUNDING TORI

organize

BRANCHED MANIFOLDS

organize

LINKS OF PERIODIC ORBITS